Magnetic Field Independent SERF Magnetometer

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SERF magnetometers based on dense ensembles of alkali-metal spins are precision quantum sensors that hold the record of measured and projected sensitivity to magnetic fields, in the $\mu G - mG$ range. At geomagnetic fields however, these sensors quickly lose their magnetic sensitivity due to spin decoherence by random spin-exchange collisions. Here we discover that atoms with nuclear spin I = 1/2 can operate in the Spin-Exchange Relaxation Free (SERF) regime but for any magnitude of the magnetic field. We counter-intuitively show that frequent collisions between a dense and optically-inaccessible (I = 1/2) gas with another optically-accessible spin gas (I > 1/2) improve the fundamental magnetic sensitivity of the latter. We analyze the performance of a dual-specie potassium and atomic hydrogen magnetometer, and project a fundamental sensitivity of about $10 \, \mathrm{aT} \sqrt{\mathrm{cm}^3/\mathrm{Hz}}$ at geomagnetic fields for feasible experimental conditions.

Precision sensing of magnetic fields is a cardinal technique in various scientific disciplines [1-11]. Warm ensembles of alkali-metal atoms feature an unprecedented sensitivity for measuring slowly varying and constant magnetic fields [12-16]. The high sensitivity of these sensors relies on the efficient coupling of the electron spin of each alkali-metal atom to the field and the use of a macroscopic ensemble that responds in a collective manner.

At geomagnetic field, the fundamental sensitivity of magnetometers based on alkali-metal atoms reaches a lower bound around $0.6 \,\mathrm{fT} \sqrt{\mathrm{cm}^3/\mathrm{Hz}}$. The dependence of this limit on the atomic number density is very weak [17], because an increase in the number of spins which probe the field leads to increased decoherence by collisions [18]. Yet, At some conditions it is possible to suppress the decoherence caused by spin-exchange collisions, which are the dominant collision process in dense ensembles of alkali atoms in their electronic ground state [13, 19, 20]. Such operation corresponds to the Spin-Exchange-Relaxation Free (SERF) regime, which features an improved fundamental sensitivity by about two orders-of-magnitudes, down to 10 $aT_{\sqrt{cm^3/Hz}}$, where the atoms response is limited by other relaxation processes [14, 21]. To date, operation in this regime at low magnetic fields holds the record of best realized magnetic sensitivity [22].

Operation in the SERF regime however poses stringent conditions on the degree of spin-polarization of the atoms [17, 23, 24], on the selectivity of the optical transitions [25], or on the magnitude of the ambient magnetic field [13–15, 26–33]. Near unity polarized spins are less susceptible to spin-exchange relaxation but typically require high optical power at pulsed operation. Operation at low magnetic fields on the other hand, requires high atomic densities, and is practically limited to a few milligauss. The low-field requirement often renders the SERF regime impractical for most applications which operate in a magnetically unshielded environment, in the presence of earth's magnetic field (a few hundreds of milligauss).

Here we propose and analyze the operation of a hydrogen-based magnetometer which operates in the SERF regime and is unrestricted to low magnetic fields. We first discover that hydrogen atoms are inherently free of spin-exchange relaxation at any magnetic field or degree of spin-polarization, owing to their simple spin structure. We then analyze the operation of a hybrid potassium-hydrogen magnetometer, which enables control and measurement of the optically inaccessible spinstate of the hydrogen ensemble through its efficient collisional coupling. We demonstrate that the potassium atoms inherit the coherent spin properties of the hydrogen, and can therefore attain an improved fundamental sensitivity down to $10 \,\mathrm{aT} \sqrt{\mathrm{cm}^3/\mathrm{Hz}}$ at high magnetic fields. We finally outline an experimentally feasible configuration for realizing such a sensor.

The main limitation on the sensitivity of warm atomic magnetometers operating at high magnetic fields originates from relaxation induced by frequent spin-exchange collisions. In the mean-field (single-spin) picture [19, 34–37], collisions predominantly alter the internal spin distribution of each atom, and drive it to follow a spintemperature distribution (STD). The ground-state energy levels of alkali-metal atoms, whose nuclear spin Iis nonzero, are split into two different hyperfine manifolds with quantum numbers F, m (with $F = I \pm S$ and $|m| \leq F$) and have a density matrix $\rho(F, m) \propto e^{\beta m}$,



Figure 1. Spin-exchange relaxation a, Frequent binary collisions of warm atomic gas lead to efficient exchange of spin. **b**. Alkali-metal atoms with a single valence electron are comprised of two hyperfine manifolds in the electronic ground-state. The total spin F precesses clockwise (counterclockwise) in the upper (lower) manifold in between sudden collisions. c-d, Spin-exchange relaxation mechanism for atoms with nuclear spin I = 3/2. c, For spin ensembles oriented along x, the populations of the spin levels follow a spin temperature distribution (STD) $\rho \propto e^{\beta m_x}$, the equilibrium state by collisions. d, Spin-precession by the magnetic field along z deters the STD, leading to decoherence by collisions; e.g. after a $\pi/2$ pulse the spin distribution is $\rho \propto e^{(-1)^F \beta m_y}$ instead, where the population in the lower hyperfine manifold is inverted. e-f, Precession of spin 1/2 atoms maintains the spin-temperature distribution at all times, thus suppressing the relaxation associated with spin-exchange collisions. **c,e**, Distributions at t = 0 with quantization axis along \hat{x} . **d**,**f**, Distributions at $t = \pi/(2\gamma B_z)$ with quantization axis along $\hat{y}_{,.}$

following STD, as shown in Fig. 1. The inverse temperature coefficient $\beta(P)$ depends on the degree of spinpolarization of the vapor $0 \leq P \leq 1$, which is a conserved quantity in the absence of other relaxation processes [38]. For this distribution and at ambient conditions, the two hyperfine manifolds are populated independently of the hyperfine energy splitting.

A magnetic field can perturb the spin-distribution of the atoms, and compete with spin-exchange collisions which act to maintain it at STD. In the presence of a magnetic field, the spins experience Larmor precession, whose rate varies between the two hyperfine manifolds. For atoms with I > 1/2, the electron spin in the upper hyperfine manifold is aligned with the field, but is anti-aligned at the lower manifold. Consequently, the total spin in the two hyperfine manifolds precess at the same rate $\gamma = \gamma_e/(2I + 1)$ but at opposite directions where $\gamma_e = 28 \text{ MHz/mT}$ is the electron gyromagneticratio. The opposite precession rates drive the system away from a spin-temperature distribution due to differential rotation of the two hyperfine manifolds. For example, a spin oriented transverse to the field and initially in a spin temperature distribution $\rho \propto e^{\beta m}$, would end in a distribution of $\rho \propto e^{(-1)^F \beta m}$ after a precession time of $\pi/(2\gamma B_z)$, as illustrated in Fig. 1d. It is this deviation from STD that causes the decoherence associated with spin-exchange collisions. For spin-ensembles aligned along the field, or when the Larmor frequencies are synchronized by optical means [25], there is no precession and therefore no spin-exchange decoherence. In the SERF regime, the deviation from STD is small; either the lower hyperfine manifold is barely populated at near unity spin-polarization, or the magnetic field perturbing the STD is weaker with respect to the spinexchange collisions rate $R \gg \gamma B$.

For atoms with I = 1/2 however, the lower hyperfine manifold is composed of a single level with m = 0 as shown in Fig. 1e-f. Consequently, a magnetic field generates precession of the magnetic moment in the upper hyperfine manifold only, and the STD is always maintained. It is therefore expected that atoms with I = 1/2would be inherently in the SERF regime, regardless of the strength of the Larmor precession γB and polarization P.

We demonstrate this inherent suppression of spinexchange relaxation for I = 1/2 for spins initially in a STD, using two different models. First, we solve the hyperfine Bloch equations for atoms with nuclear spin I, and describe the dynamics of the average spin of the two hyperfine manifolds in the low polarization limit [19, 25, 39]. These equations account for the magnetic field precession at a rate γB , spin exchange collisions at a rate $R = 10^6 \,\mathrm{s}^{-1}$, and taking a fixed longitudinal spin lifetime $T_1 = 10 \text{ ms}$ for all values of I. In Fig. 2(ab) we present the decoherence rate Γ for spins oriented transverse to the field and gyromagnetic ratio $\gamma_{\rm eff}$ as a function of magnetic field. For I > 1/2 atoms, at high magnetic fields ($\gamma B \gg R$, practically including also geomagnetic fields, denoted by a dashed vertical line), the relaxation is dominated by spin-exchange collisions and is suppressed only at low magnetic fields. I = 1/2atoms in contrast, feature a constant and reduced decoherence rate which is solely governed by their finite lifetime. The gyro-magnetic ratio for I = 1/2 atoms is also independent of the magnetic field, unlike all other atoms experiencing spin-exchange collisions.

To further validate the inherent SERF property of I = 1/2 atoms we explore an additional model. We solve the Unitary spin-exchange evolution for pairs of alkali-like spins initially in a STD. During a collision, the two valence electrons of a pair decompose into a Singlet and Triplet states, which acquire different phases, where their relative phase ϕ governs the transition amplitudes of the evolution. At room-temperature and



Figure 2. Suppression of Spin-Exchange relaxation and frequency slowing-down for I = 1/2 atoms. a, The transverse decoherence rate Γ of I > 1/2 atoms is dominated by spin-exchange at high magnetic field B. In contrast, the relaxation rate of I = 1/2 atoms (blue) is highly suppressed at all magnetic fields; it is determined by the finite lifetime but independent of the spin-exchange rate R .b, The gyromagnetic-ratio γ depends on magnetic field magnitude for all atoms but I = 1/2. c, Single events of spin-exchange collisions with relative scattering phase ϕ between the singlet and triplet states redistribute the magnetic coherence for all I = 3/2, mostly at low degrees of polarization P, but not for I = 1/2 (at any P). The unitless parameter ϵ quantifies the distribution of the magnetic coherence between the hyperfine manifold by collisions (See text). d, In the weak field limit ($\gamma_e B \ll R$), the gyromagnatic-ratio of I > 1/2 atoms depends on the degree of spin polarization, but is constant for I = 1/2 atoms. The gyromagnatic-ratio determines the slowing-down factor $q = \gamma_e/\gamma$. a-b are obtained from the hyperfine Bloch equations in the low polarization regime and c-d from a numerical stochastic model.

above, ϕ is almost uniformly distributed between 0 to 2π [21, 40–43]. The outcome of a collision for an initial two-body density matrix $\rho_a \otimes \rho_b$ is then given by [21, 44]

$$\rho = \Pi_{\rm T} \rho_a \otimes \rho_b \Pi_{\rm T} + e^{i\phi} \Pi_{\rm S} \rho_a \otimes \rho_b \Pi_{\rm S}, \qquad (1)$$

where $\Pi_{\rm S}$ and $\Pi_{\rm T}$ are the projection operators on the singlet and triplet states respectively. We estimate the average amount of spin transfer between the two hyperfine states by the unitless quantity $\epsilon^a_+ =$ $(\langle F_{\rm out}^{(+a)} \rangle - \langle F_{\rm in}^{(+a)} \rangle)/(\langle F_{\rm in}^{(+a)} \rangle + \langle F_{\rm in}^{(+b)} \rangle)$ which is presented in Fig. 2c., using $\langle F_{\rm (in/out)}^{(+a)} \rangle = \text{Tr}(\rho F_+^{(a)})$. For I = 3/2 atoms, $\epsilon^a_+ > 0$ and the magnetic moments are redistributed by collisions, depending on the value of ϕ . The spin at the upper hyperfine manifold for I = 1/2atoms in contrast, is unaffected for any ϕ .

We further extend our previous numerical estimations of the gyromagnetic ratio and relaxation rate for any degree of spin-polarization. We simulate the Unitary magnetic evolution of pairs of atoms in between collisions, but to keep the computational space tractable, trace out the inter-atomic coherence developed after each collision with a random ϕ by setting $\rho \to \text{Tr}_b(\rho) \otimes \text{Tr}_a(\rho)$. We characterize the gyromagnetic ratio as a function of the spin-polarization P in the low magnetic field regime and show it in Fig. 2d, where $q = \gamma/\gamma_e$ denotes the slowing-down factor [38]. While the effective gyro magnetic ratio depends on the polarization P for all I > 1/2atoms, it is independent of P for I = 1/2. We verify convergence and confirm the agreement of this model with the hyperfine-Bloch equations in the low polarization regime.

The hydrogen atom has a single valence electron and its nuclear spin is I = 1/2. It could therefore be utilized as an inherent SERF magnetometer. Its most stable form appears as a molecule H₂, which can be efficiently dissociated via e.g., application of highfrequency RF discharge. Once dissociated, it can maintain its atomic form for long time before associating back into a molecule as this process typically requires three bodies [45–51]; 1 Torr of atomic hydrogen in a cmsize enclosure can last about a hundred of milliseconds, as traditionally utilized in precision masers [52–56].

A primary challenge in usage of atomic hydrogen relates to its energetic excited state, which hinders optical manipulation or readout of its ground state using standard laser frequencies, since its optical transitions are in the UV. Masers overcome this challenge by using nonoptical methods [57–59]; pumping the hydrogen spins using permanent magnets in a Stern-Gerlach configuration, and reading their state using microwave cavities. Here we consider another approach based on a hybrid



Figure 3. Operation of a dual potassium-hydrogen magnetometer. a, Configuration of a dual-specie magnetometer. Atomic hydrogen (I = 1/2) precesses around a magnetic field $B_z \hat{z}$ using a weak magnetic drive $B_{\perp} \cos(\omega t) \hat{x}$, and imprints its precession on a dilute potassium spin gas (I = 3/2). The optically-controlled potassium spins continuously polarize and read the state of the hydrogen spins. **b**, Calculated magnetic response of the potassium spins to the oscillatory magnetic drive. The potassium spins, dressed by the interaction with the hydrogen spins, feature a double resonance spectrum with resonance frequencies $\omega_{\rm K}$ and $\omega_{\rm H} = 2\omega_{\rm K}$, as shown in red line for a low hydrogen density. At optimal conditions, the hydrogen density is higher and the imprinted hydrogen response dominates the potassium magnetic spectrum (blue line). Red and blue lines correspond to cross and star symbols in Fig. 4.

configuration where the hydrogen is collisionally coupled to another optically accessible ensemble of alkali-metal atoms [60–63].

We consider a gaseous mixture of atomic hydrogen with potassium atoms (I = 3/2) as illustrated in Fig. 3a. The potassium spin-polarization vector \mathbf{P}_{K} is opticallypumped continuously along the magnetic field $B_z \hat{z}$, and its transverse component in the xy plane can be optically probed using standard techniques [64, 65]. The potassium spins are coupled to the ensemble of hydrogen spins with mean polarization vector \mathbf{P}_{H} via mutual spin exchange collisions, which act to equilibrate the spin-polarization of the two ensembles.

This collisional coupling enables pumping of the hydrogen spins and also imprinting their precession on the measured response of the potassium. We can force the hydrogen precession by application of a weak and transverse magnetic field $B_{\perp} \cos(\omega t)\hat{x}$, whose modulation is

resonant with the hydrogen frequency $\omega_{\rm H} = \gamma_{\rm H} B$ but off resonant from the potassium $\omega_{\rm K} = \gamma_{\rm K} B = \omega_{\rm H}/2$ at high magnetic fields. Including spin-relaxation of the valence electron for both species at rates $R_{\rm sd}^{\rm K}$, $R_{\rm sd}^{\rm H}$ and optical pumping of the potassium electrons at rate $R_{\rm p}$ along \hat{z} , we can describe the coupled dynamics with the set of Bloch equations

$$\begin{aligned} \mathbf{P}_{\mathrm{H}} &= \gamma_{\mathrm{H}} \mathbf{B} \times \mathbf{P}_{\mathrm{H}} + \Gamma_{\mathrm{HK}} \mathbf{P}_{\mathrm{K}} - \Gamma_{\mathrm{H}} \mathbf{P}_{\mathrm{H}} + \boldsymbol{\xi}_{\mathrm{H}}, \\ \dot{\mathbf{P}}_{\mathrm{K}} &= \gamma_{\mathrm{K}} \mathbf{B} \times \mathbf{P}_{\mathrm{K}} + \Gamma_{\mathrm{KH}} \mathbf{P}_{\mathrm{H}} - \Gamma_{\mathrm{K}} \mathbf{P}_{\mathrm{K}} + \Gamma_{\mathrm{p}} \hat{z} + \boldsymbol{\xi}_{\mathrm{K}}. \end{aligned}$$
(2)

Here $\mathbf{B}(t) = B_z \hat{z} + B_\perp \cos(\omega t) \hat{x}$ denotes the total magnetic field vector and $\Gamma_{\rm HK} = k_{\rm HK} n_{\rm K}/q_{\rm H}$ and $\Gamma_{\rm KH} = k_{\rm HK} n_{\rm H}/q_{\rm K}$ are the hybrid spin-exchange rates, where $n_{\rm K}, n_{\rm H}$ are the potassium and hydrogen numberdensities, $k_{\rm HK} = 5.4 \times 10^{-10} \text{ cm}^3/\text{s}$ is the mutual spinexchange rate coefficient [61] and $q_{\rm H}$ and $q_{\rm K}$ are the slowing-down factors of the two species [38] presented in Fig. 2d. We take $\Gamma_{\rm p} = R_{\rm P}/q_{\rm K}$ as the optical pumping rate and $\Gamma_{\rm K} = \Gamma_{\rm p} + \Gamma_{\rm KH} + (R_{\rm sd}^{\rm K} + R_{\rm se}^{\rm K})/q_{\rm K}$ and $\Gamma_{\rm H} = \Gamma_{\rm HK} + R_{\rm sd}^{\rm H}/q_{\rm H}$ as the transverse relaxation rates of the two ensembles. The hydrogen spins relax by spindestruction processes or spin-exchange collisions with the potassium spins, but crucially, are free of spinexchange relaxation by rapid collisions with other hydrogen atoms (i.e., $R_{\rm se}^{\rm H} = 0$).

We introduce the white noise vector processes $\boldsymbol{\xi}_{\mathrm{H}}$ and $\boldsymbol{\xi}_{\mathrm{K}}$ transverse to the polarization axis to describe the Atom Projection Noise (APN) that limits the fundamental sensitivity of the magnetometer (i.e. the standard quantum limit) [32, 66]. They satisfy $\langle \boldsymbol{\xi}_{\mathrm{H}}(t) \rangle = \langle \boldsymbol{\xi}_{\mathrm{A}}(T) \rangle = 0$ but have a nonzero variance $\langle \xi_{\mathrm{qi}}(t) \xi_{\mathrm{q'j}}(t') \rangle = \delta_{ij} \delta_{qq'} \delta(t-t') R_q/(n_q V)$ for $q, q' \in$ {K, H} and $i, j \in \{x, y\}$.

We begin by presenting an approximate analytical solution of Eqs. (2) to illustrate the coupled dynamics, and then present more general numerical results. We consider the regime in which the Hydrogen is the dominant specie $n_{\rm H} \gg n_{\rm K}$ and assume the rotating wave approximation such that $\omega \gtrsim \Gamma_{\rm K}, \Gamma_{\rm KH} \gg \Gamma_{\rm H}$. By continuous optical pumping the potassium spins reach a steady polarization of

$$P_{\mathrm{K}z} = \frac{\Gamma_{\mathrm{p}}\Gamma_{\mathrm{H}}}{\Gamma_{\mathrm{K}}\Gamma_{\mathrm{H}} - \Gamma_{\mathrm{KH}}\Gamma_{\mathrm{HK}}}.$$
(3)

Sizeable polarization requires pumping rate that scales as $\Gamma_{\rm p} \sim n_{\rm H} k_{\rm HK}$, accounting for the transfer of spin polarization from the rare potassium vapor to the dense hydrogen gas. In the presence of the weak driving field $\gamma_{\rm H} B_{\perp} \lesssim \Gamma_{\rm H}$, the mean response of the transverse potassium spin $\langle P_{\rm K+} \rangle = \langle P_{\rm Kx} + i P_{\rm Ky} \rangle$ at the drive frequency ω is dominated by the coupling to the driven hydrogen and in the rotating frame is given by



Figure 4. **Projected Fundamental sensitivity.** The magnetic sensitivity of the hydrogen-potassium magnetometer limited by atom-projection noise, and independent of the magnetic field magnitude. Cross and star correspond to the configurations presented in Fig. 3b in red and blue lines respectively.

$$\langle P_{\mathrm{K}+}(\omega)\rangle = \frac{i\gamma_{\mathrm{K}}B_{\perp}P_{\mathrm{Kz}}}{\Gamma_{\mathrm{H}}(1 - \frac{(\Gamma_{\mathrm{K}} - i(\omega_{\mathrm{K}} - \omega))}{\Gamma_{\mathrm{KH}}}\frac{(\Gamma_{\mathrm{H}} - i(\omega_{\mathrm{H}} - \omega))}{\Gamma_{\mathrm{HK}}})}.$$
 (4)

The spectral response of Eq. (4) has a double resonance shape, a broad complex Lorentzian centered at $\omega_{\rm K}$ with linewidth $\Gamma_{\rm K}$, and a narrow complex Lorentzian centered at $\omega_{\rm H}$ and linewidth $\Gamma_{\rm H}$, as shown in Fig. 3b (red line). The former corresponds to the response of the potassium to oscillations at its bare resonance, which is broadened by rapid collisions with the hydrogen and optical pumping. The latter and stronger resonance, manifests the efficient response of hydrogen atoms to the field, imprinted on the potassium response by rapid spin-exchange collisions.

The narrow resonance line at $\omega = \omega_{\rm H}$ is associated with a sharp variation of the phase of $\langle P_{\rm K+} \rangle$ which in turn allows for sensitive estimation of the resonance frequency $\omega_{\rm H}$ and therefore of the magnetic field B_z . We estimate the magnetic sensitivity in this configuration due to APN by linearizing the response of Eq. (4) around $\omega - \omega_{\rm H}$ and computing the APN variance, see Appendix A. To reveal the qualitative scaling of the magnetic noise, we assume the simplifying conditions $\Gamma_{\rm H} \sim \Gamma_{\rm HK}$ and $\Gamma_{\rm K} \sim \Gamma_{\rm KH}$ and find that for a measurement volume V, the spin variance of the potassium scales as $\langle |\Delta P_{\rm K+}(\omega = \omega_{\rm H})|^2 \rangle \propto t/(\Gamma_{\rm H} n_{\rm H} V)$, and the fundamental magnetic sensitivity is limited by the effective magnetic noise

$$\delta B_{\rm APN} \propto \frac{1}{\gamma_{\rm H}} \sqrt{\frac{\Gamma_{\rm H}}{n_{\rm H} V}}.$$
 (5)

Remarkably, the fundamental sensitivity in this configuration is determined by the Hydrogen properties: its high number-density and its narrow linewidth, therefore enabling high sensitivity at large magnetic fields $\gamma_{\rm H}B \gg \Gamma_{\rm H}$. Comparison of this response to a singlespecie potassium magnetometer, whose low density is tuned to set $\Gamma_{\rm K} = \Gamma_{\rm H}$, reveals that the sensitivity in the proposed hybrid configuration is enhanced by a large factor that scales as $\sqrt{n_{\rm H}/n_{\rm K}}$.

To quantitatively analyze the magnetometer performance, we numerically calculate the fundamental sensitivity as a function of $n_{\rm K}$ and $n_{\rm H}$, and at each point optimize for the optical pumping rate $\Gamma_{\rm p}$ and the amplitude of the magnetic drive B_{\perp} . We take $\Gamma_{\rm H} = 40 \, {\rm s}^{-1}$ and present the calculated fundamental sensitivity in Fig. 4. We find a fundamental magnetic sensitivity of $\delta B_{\rm APN} = 10 {\rm aT} \sqrt{{\rm cm}^3/{\rm Hz}}$ as marked by a cyan star for $n_{\rm K} = 1.2 \times 10^{11} \, {\rm cm}^{-3}$, $n_{\rm H} = 2.7 \times 10^{16} \, {\rm cm}^{-3}$ using $B_{\perp} = 0.35 \, {\rm nT}$ and $\Gamma_p = 1.2 \times 10^7 \, {\rm s}^{-1}$, which correspond to about 1.5 W of pump beam power in a 1" diameter cell. The spectral response of the potassium at these conditions is plotted in Fig. 3 with a blue line and the configuration associated with the red line is marked with a red cross in Fig. 4.

In summary, we proposed and analyzed using the mixture of hydrogen-potassium atoms for a precision optical magnetometer. Owing to their simple spin structure, hydrogen atoms (I = 1/2) are free of spin-exchange relaxation at any magnetic field and spin-polarization, enabling the potential operation of this magnetometer in the ultra-sensitive SERF regime at geomagnetic fields.

It is interesting to compare the operation of this hybrid magnetometer with other precision dual species sensors such as alkali-metal and noble gas comagnetometers [2, 64, 67, 68]. In comagnetometers, the alkali spin is utilized for pumping and probing of noble-gas spins, which are used for precision sensing of external fields. The coupling between noble-gas atoms to alkalimetal spins relies on the weak Fermi-contact interaction, and can attain high sensitivity which is limited to an ultranarrow bandwidth set by their long lifetime [1, 6, 69]. Our configuration in contrast, relies on strong exchange interaction between the valence electrons of the two species, and the efficient response of the hydrogen atoms to magnetic fields.

Furthermore, the hybrid hydrogen-potassium configuration is potentially more accurate with respect to other single-specie SERF magnetometers; The hydrogen's gyromagnetic ratio is known to a high accuracy, and unlike atoms with I > 1/2, it is independent of the degree of spin polarization or magnitude of the magnetic field.

Finally, it is intriguing to consider the operation of this configuration from a spin-noise perspective. The spin noise of dual specie configurations has been analyzed theoretically and experimentally in [66], demonstrating that spin-exchange coupling with another specie acts to increase the measured noise variance. Here we also find that the potassium spin-projection noise is increased by a factor $\sim \sqrt{n_{\rm H}/n_{\rm K}}$. It is the improvement of the potassium signal by a larger factor $\sim n_{\rm H}/n_{\rm K}$ that leads to the enhanced sensitivity of this hybrid sensor. The dressed hydrogen-potassium state can potentially also be implemented in other emerging avenues such as in efficient generation of spinentanglement [28, 70–73] and other quantum optics applications [74–77].

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